



# basic education

Department:  
Basic Education  
REPUBLIC OF SOUTH AFRICA

**NATIONAL  
SENIOR CERTIFICATE**

**GRADE 12**

**MATHEMATICS P3  
NOVEMBER 2011  
MEMORANDUM**

MARKS: 100

**DEPARTMENT OF BASIC  
EDUCATION**  
  
2011 -11- 02  
PRIVATE BAG X 110  
PRETORIA 0001  
**PUBLIC EXAMINATIONS**

This memorandum consists of 14 pages.

*Approved*  
*M. Sasman*  
07 November 2011

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*[Signature]*  
07/11/2011

*Approved*  
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7/11/2011

Please turn over

**NOTE:**

- If a candidate answers a question TWICE and does not delete any attempt, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent Accuracy applies in ALL aspects of the marking memorandum.
- A learner cannot use what s/he must prove to prove it (i.e. the circular argument.).

**QUESTION 1**

<p>1.1</p>	<p><math>T_{k+1} = T_k - 2; k \geq 1; T_1 = 12</math></p> <p><math>T_1 = 12</math>  <math>T_2 = 12 - 2 = 10</math>  <math>T_3 = 10 - 2 = 8</math>  <math>T_4 = 8 - 2 = 6</math></p>	<p>✓ 10                  ✓ 8                  ✓ 6</p> <p>(3)</p>
<p>1.2</p>	<p><math>12 + 10 + 8 + 6 + 4 + 2 + 0 + (-2) + (-4) + (-6) + (-8) + (-10) + (-12)</math>  <math>= 0</math>  <math>\therefore 13</math> terms</p> <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <p><b>Note:</b>                      If a learner writes out  <math>12 + 10 + 8 + 6 + 4 + 2 + 0</math>                      then 1/3 marks</p> </div> <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <p><b>Note:</b>                      Answer only: FULL marks</p> </div> <p><b>OR</b></p> <p>There are 6 positive terms before the 7th term, which is 0. We need 6 negative terms of equal value to the positive terms so that the sum is zero</p> <p>6 positive terms + 1 zero term + 6 negative terms  <math>= 13</math> terms</p> <p><b>OR</b></p> <p><math>\frac{n}{2}[2(12) + (n-1)(-2)] = 0</math>  <math>\frac{n}{2}[24 + 2 - 2n] = 0</math>  <math>\frac{n}{2}[26 - 2n] = 0</math>  <math>13n - n^2 = 0</math>  <math>n(13 - n) = 0</math>  <math>n \neq 0</math> or <math>n = 13</math></p>	<p>✓ expansion                  ✓ 13 terms</p> <p>(3)</p> <p>✓ <math>T_7 = 0</math>                  ✓ 12 terms                  ✓ 13 terms</p> <p>(3)</p> <p>✓ substitution into the arithmetic sum formula                  ✓ <math>\frac{n}{2}[26 - 2n] = 0</math></p> <p>✓ 13 terms</p> <p>(3) (6)</p>

*MS* *8*

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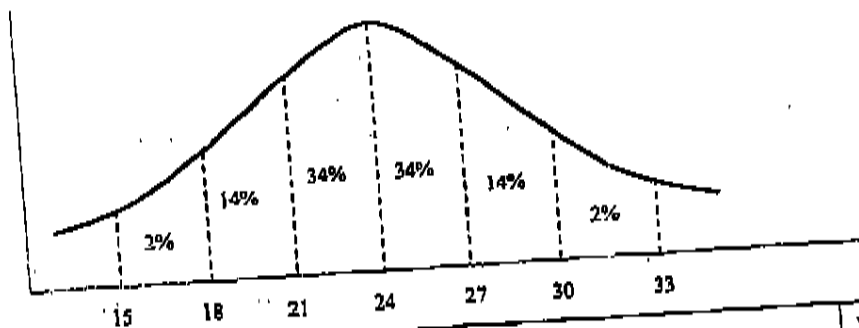
## QUESTION 2

2.1	$42 - 28 = 14$	✓ answer (1)
2.2	Approximately 88 kg	✓ answer (1)
2.3	<p><b>NOTE:</b> Accept a range from 86 to 89 kg</p> <p>15 learners in the sample have a weight of less than 80 kg. One would expect <math>\frac{15}{50} \times 250 = 75</math> learners in the grade to have a weight of less than 80 kg.</p> <p><b>OR</b></p> <p>15 learners in the sample have a weight of less than 80 kg. One would expect <math>15 \times 5 = 75</math> learners in the grade to have a weight of less than 80 kg.</p> <div style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <p><b>NOTE:</b></p> <ul style="list-style-type: none"> <li>• Accept <math>\frac{14}{50} \times 250 = 70</math></li> <li>• Answer as percentage: 1/2 marks</li> <li>• Answer only: 2/2 marks</li> </ul> </div>	<p>✓ Cumulative Frequency value read off the graph when less than 80 ✓ answer (2)</p> <p>✓ Cumulative Frequency value read off the graph when less than 80 ✓ answer (2)</p>
2.4	This sampling method is biased towards those who arrive early on a Monday morning. In this way all the learners in the Grade do not have the same chance of being selected for the sample.	✓ sensible explanation of random sample (1) [5]

## QUESTION 3

3.1	<p>For mutually exclusive events</p> $P(A \text{ or } B) = P(A) + P(B)$ $0,7 = 0,4 + k$ $k = 0,3$ <div style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <p><b>Note:</b> Answer only: FULL marks</p> </div> <p><b>NOTE:</b> If the candidate writes down <math>k = 1 - 0,7 = 0,3</math>: 0/2 marks</p>	<p>✓ <math>0,7 = 0,4 + k</math> ✓ answer (2)</p>
3.2	<p>For independent events</p> $P(A \text{ and } B) = P(A) \cdot P(B)$ $= 0,4k$ $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$ $0,7 = 0,4 + k - 0,4k$ $0,3 = 0,6k$ $k = 0,5$ <p><b>OR</b></p> $0,7 = 0,4 + k - 0,4k$ $0,3 = 0,6k$ $k = 0,5$ <div style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <p><b>Note:</b></p> <ul style="list-style-type: none"> <li>• Answer only: 1/4 marks</li> <li>• Wrong formula: 0/4 marks</li> </ul> </div>	<p>✓ <math>P(A \text{ and } B) = P(A) \cdot P(B)</math> ✓ <math>0,4k</math> ✓ <math>0,7 = 0,4 + k - 0,4k</math> ✓ answer (4)</p> <p>✓✓✓ <math>0,7 = 0,4 + k - 0,4k</math> ✓ answer (4) [6]</p>

## QUESTION 4



4.1	21 minutes is 1 standard deviation from the mean ∴ 34% of the pizzas are delivered between 21 and 24 minutes  <b>Note:</b> Answer only: FULL marks	✓ 1 standard deviation ✓ 34%  (2)
4.2	15 minutes is 3 standard deviations to the left of the mean ∴ 50% 27 minutes is 1 standard deviation to the right of the mean ∴ 34% 84% of the pizzas are delivered between 15 and 27 minutes  <b>OR</b> $2\% + 14\% + 34\% + 34\%$ $= 84\%$  <b>Note:</b> Answer only: FULL marks	✓ 50% ✓ 34% ✓ 84%  (3)  ✓ 50% ✓ 34% ✓ 84%  (3)
4.3	The required 2% is the area found to the right of 2 standard deviations on the right hand side of the mean. Maximum for delivery should be $24 + 2(3)$ $= 30$ minutes  <b>Note:</b> Answer only: FULL marks	✓ 2 standard deviations ✓ $24 + 2(3)$ ✓ 30  (3) <b>[8]</b>

## QUESTION 5

5.1	Number of unique codes $= 7 \times 7 \times 7$ $= 7^3$ $= 343$  <b>Note:</b> Answer only: FULL marks	✓ $7 \times 7 \times 7$ ✓ answer  (2)
5.2	Number of unique codes without repetition $= 7 \times 6 \times 5$ $= 210$  <b>OR</b> $\frac{7!}{4!}$ $= 210$  <b>Note:</b> Answer only: FULL marks	✓ $7 \times 6 \times 5$ ✓ answer  (2)  ✓ $\frac{7!}{4!}$ ✓ answer  (2)
5.3	Number of codes with repetition that are greater than 300 and divisible by 5 $= 4 \times 7 \times 2 - 1$ $= 55$  <b>OR</b> For a 100 numbers there are 14 numbers divisible by 5 $14 \times 4 = 56$ $56 - 1 = 55$  <b>Note:</b> • No CA marking for the answer. • Answer only 3/3 marks	✓ $4 \times 7 \times 2$ ✓ - 1 ✓ answer  (3)  ✓ $14 \times 4$ ✓ - 1 ✓ answer  (3) <b>[7]</b>

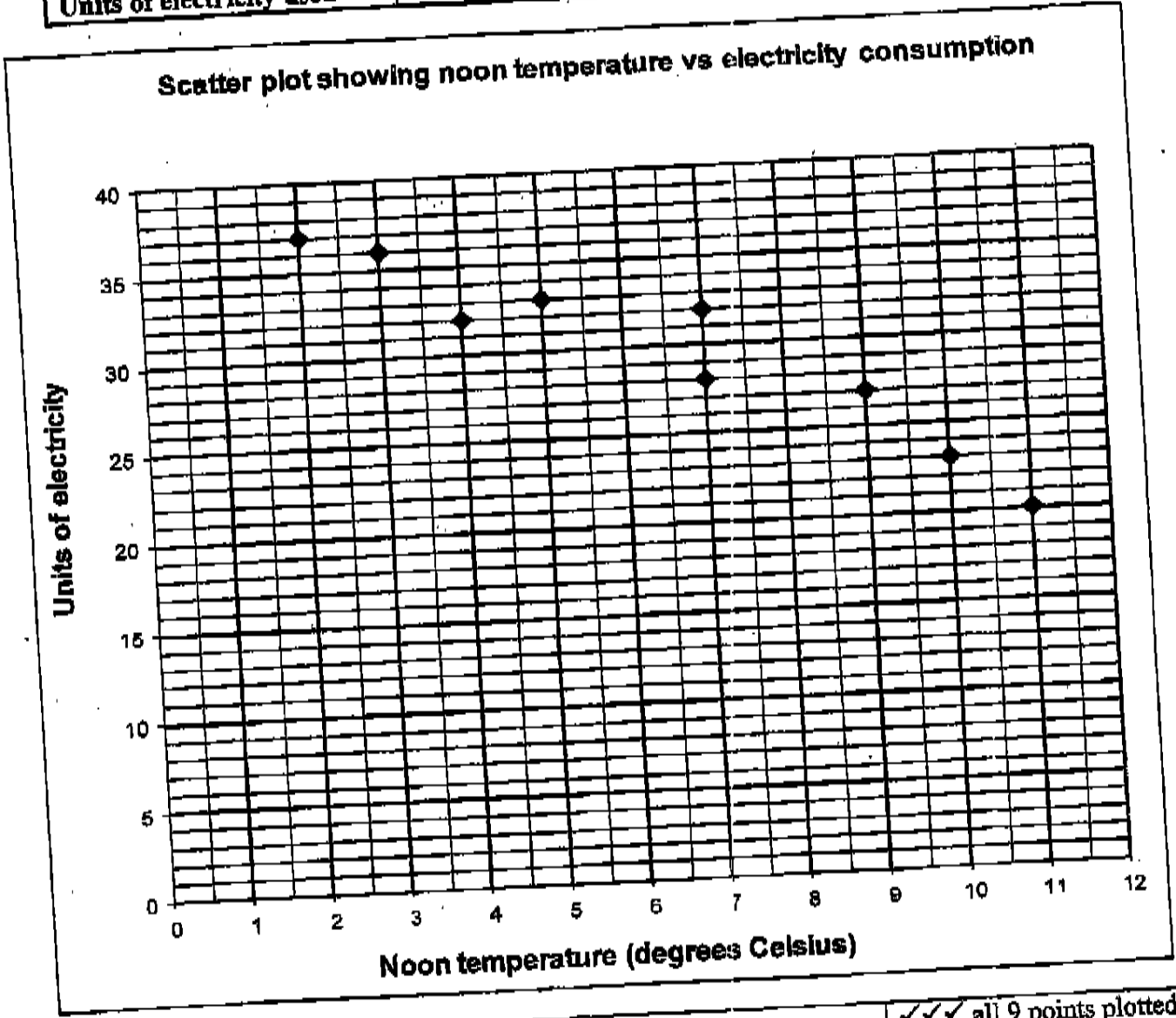
QUESTION 6

<p>6.1</p>		<p>                 ✓ 79 - x                  ✓ 20                  ✓ 19 - x                  ✓ 11                  ✓ 16                  ✓ 40 - x             </p> <p>(6)</p>
<p>6.2</p>	<p> <math>79 - x + 20 + x + 11 + 19 - x + 16 + 40 - x = 173</math>  <math>185 - 2x = 173</math>  <math>x = 6</math> </p> <p><b>OR</b>                  232 complaints and 173 people in total                  94 complaints from 47 people                  138 complaints from remaining 126 people                  For the two to be equal  <math>126 - x = 138 - 3x</math>  <math>2x = 12</math>  <math>x = 6</math> </p> <p><b>OR</b>  <math>110 + 55 + 67 = 232</math>  <math>2x + 20 + 11 + 16 = 232 - 173</math>  <math>2x + 47 = 59</math>  <math>2x = 12</math>  <math>x = 6</math> </p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p><b>Note:</b> Check the reasonableness of the answer.</p> </div>	<p>                 ✓ addition                  ✓ 173                  ✓ answer             </p> <p>(3)</p> <p>                 ✓ 126 - x and 138 - 3x                  ✓ 126 - x = 138 - 3x                  ✓ answer             </p> <p>(3)</p> <p>                 ✓ 232                  ✓ 2x + 20 + 11 + 16 = 232 - 173                  ✓ answer             </p> <p>(3)</p>
<p>6.3</p>	<p>                 P(at least two complaints)  <math display="block">= \frac{11 + 20 + 6 + 16}{173}</math> <math display="block">= \frac{53}{173}</math> <math display="block">= 0,31 \quad (0,30635838\dots)</math> <p>OR 30,64%</p> </p>	<p>                 ✓ 11 + 20 + 6 + 16                  ✓ 173             </p> <p>                 ✓ answer             </p> <p>(3) [12]</p>

*MS*

QUESTION 7

Noon temperature (in °C)	2	3	4	5	7	7	9	10	11
Units of electricity used	37	36	32	33	32	28	27	23	20



7.1 See scatter plot above

**Note:**  
Please ignore the point (0 ; 41).

✓✓✓ all 9 points plotted correctly  
2 marks if 5 - 8 points are plotted correctly  
1 mark if 1 - 4 points are plotted correctly.  
(3)

*MS 46*

*P*

7.2	$a = 40,97$ (40,97108844...) $b = -1,74$ (-1,736394558...) $\hat{y} = 40,97 - 1,74x$	✓✓ a ✓ b ✓ equation (4)
<b>Note:</b> <ul style="list-style-type: none"> <li>Penalise 1 mark for incorrect rounding to ONE decimal place in either 7.2 or 7.3</li> <li>Answer only: FULL marks</li> </ul>		
<b>NOTE:</b> If the candidate works the coefficients out manually that $b = \frac{-204,2}{117,6}$ then 2 marks for b.		
7.3	$r = -0,97$ (-0,9699269087...)  <b>NOTE:</b> If the candidate gives $b = \frac{6,139218}{3,42928}r$ and not simplified then 1 mark.	✓✓ answer (2)
7.4	There is a strong negative correlation between the noon temperature and the units of electricity used.  <b>OR</b> As the noon temperature increases, the units of electricity used decreases.  <b>OR</b> As the noon temperature decreases, the units of electricity used increases.	✓ strong ✓ negative (2)  ✓✓ as noon temp increases & units decrease (2)  ✓✓ as noon temp decreases & units increases (2)
7.5	$\hat{y} \approx 40,97 - 1,74(8)$ $\approx 27,05$  <b>OR</b> $\hat{y} \approx 27,0799 \approx 27,08$	✓ substitution ✓ answer (2) [13]
<b>Note:</b> <ul style="list-style-type: none"> <li>Answer only: 2/2 marks</li> <li>Accept a range of 26,5 – 27,5 if the least squares regression line is drawn and the answer is read off: 2/2 marks</li> </ul>		

MS

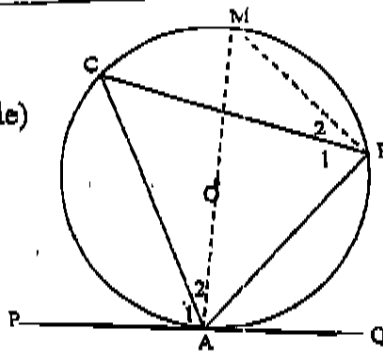
B

**QUESTION 8**

8.1

Draw diameter AM and join M to B.

- $\hat{A}_1 + \hat{A}_2 = 90^\circ$  (rad  $\perp$  tangent)
- $\hat{B}_1 + \hat{B}_2 = 90^\circ$  ( $\angle$ s in a semi circle)
- $\hat{B}_2 = \hat{A}_2$  ( $\angle$ s in same seg)
- $\hat{B}_1 = \hat{A}_1$



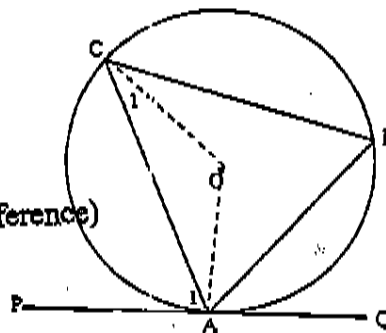
- ✓ construction
- ✓ S/R
- ✓  $\hat{B}_1 + \hat{B}_2 = 90^\circ$
- ✓  $\angle$ s in a semi circle
- ✓ S/R

(5)

**OR**

Draw radii OC and OA

- Let  $\hat{A}_2 = x$
- $\hat{C}_1 = x$  ( $\angle$  opp = radii)
- $\hat{A}_1 = 90^\circ - x$  (rad  $\perp$  tan)
- $\angle AOC = 180^\circ - 2x$  ( $\angle$  sum  $\Delta$ )
- $\angle ABC = 90^\circ - x$  ( $\angle$  circ cent = 2  $\angle$  circumference)
- $\angle ABC = \hat{A}_1$  ( $= 90^\circ - x$ )



- ✓ construction
- ✓  $\hat{A}_1 = 90^\circ - x$
- ✓ rad  $\perp$  tan
- ✓ S/R
- ✓ S/R

(5)

**NOTE:**

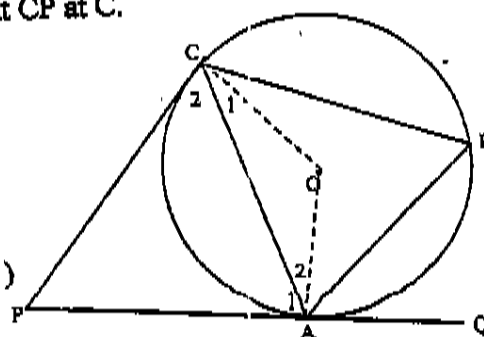
If there is no construction: 0 / 5 marks

If candidate changes lettering and states "Similarly": full marks

**OR**

Draw QA extend to P. Draw tangent CP at C.

- $PC = PA$  (tan from comm pt)
- $\hat{C}_2 = \hat{A}_1$  ( $\angle$ s opp = sides)
- $\angle COA = 2\angle ABC$
- ( $\angle$  circ cent = 2  $\angle$  circumf)
- $\hat{A}_1 + \hat{A}_2 = 90^\circ$  (tan  $\perp$  radius)
- $\angle COA = 180^\circ - (90^\circ - \hat{A}_1 + 90^\circ - \hat{C}_2)$
- $= \hat{A}_1 + \hat{C}_2$
- $= \hat{A}_1 + \hat{A}_1$
- $= 2\hat{A}_1$
- $\hat{A}_1 = \frac{1}{2}\angle COA$
- $= \angle CBA$



- ✓ construction
- ✓ S/R

✓ S/R

- ✓  $\hat{A}_1 + \hat{A}_2 = 90^\circ$
- ✓ tan  $\perp$  radius

(5)

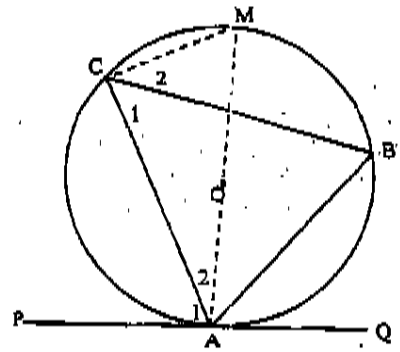
**OR**

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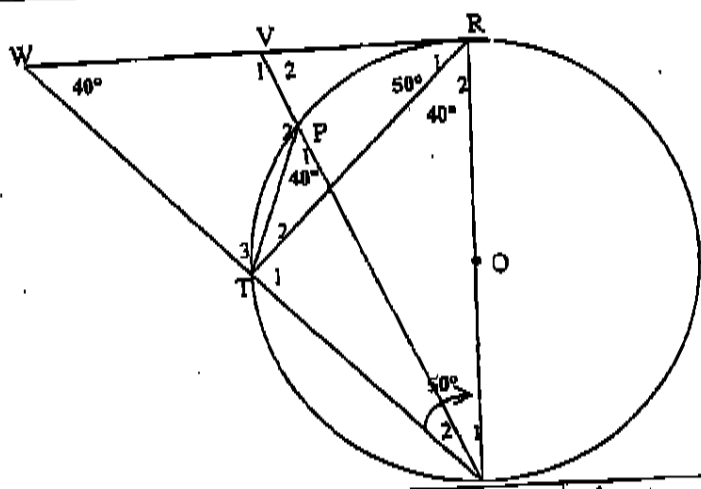


Draw diameter AM and Join M and C  
 $\widehat{MCA} = 90^\circ$  ( $\angle$ s in semi circle)  
 $\widehat{AMC} + \widehat{A}_2 = 90^\circ$  ( $\angle$  sum  $\Delta$ )  
 $\widehat{A}_1 + \widehat{A}_2 = 90^\circ$  (rad  $\perp$  tangent)  
 $\widehat{AMC} = \widehat{A}_1$   
 $\widehat{AMC} = \widehat{B}$  ( $\angle$ s in same seg)  
 $\widehat{A}_1 = \widehat{B}$



- ✓ construction
- ✓ S/R
- ✓ S/R
- ✓  $\widehat{A}_1 + \widehat{A}_2 = 90^\circ$
- ✓ tan  $\perp$  radius

(5)



8.2.1	$\widehat{WRS} = 90^\circ$ (tan $\perp$ radius)	✓ statement (1)
8.2.2	$\widehat{RST} = 50^\circ$ (tan ch th) $\widehat{W} = 40^\circ$ ( $\angle$ sum $\Delta$ )	✓ S/R ✓ $\widehat{W} = 40^\circ$ (2)
	<b>OR</b> $\widehat{T}_1 = 90^\circ$ ( $\angle$ s in semi circle) $\widehat{W} + \widehat{R}_1 = \widehat{T}_1$ (ext $\angle$ $\Delta$ ) $\widehat{W} = 40^\circ$	✓ $\widehat{W} + \widehat{R}_1 = \widehat{T}_1$ ✓ $\widehat{W} = 40^\circ$ (2)
8.2.3	$\widehat{R}_2 = 40^\circ$ (tan $\perp$ radius) $\widehat{P}_1 = 40^\circ$ ( $\angle$ s in same seg)	✓ $\widehat{R}_2 = 40^\circ$ ✓ $\widehat{P}_1 = 40^\circ$ ✓ $\angle$ s in same seg (3)

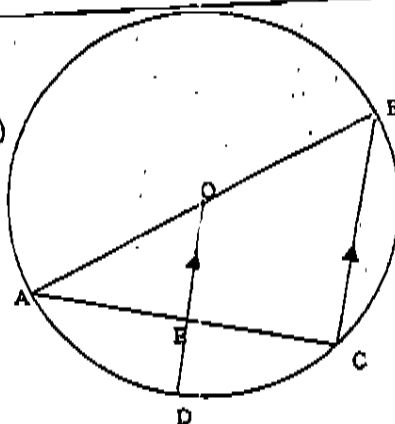
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<p>8.2.4 <math>\hat{P}_1 = \hat{W}</math> (<math>= 40^\circ</math>)  WVPT is a cyclic quadrilateral (ext <math>\angle =</math> int opp)  <math>\hat{V}_1 = \hat{P}\hat{T}\hat{S}</math> (ext <math>\angle</math> cyclic quad)</p> <p>OR</p> <p><math>\hat{T}_1 = 90^\circ</math> (<math>\angle</math>s in semi circle)  <math>\hat{P}\hat{T}\hat{S} = 90^\circ + \hat{T}_2</math>  <math>\hat{T}_2 = \hat{S}_1</math> (<math>\angle</math>s in same seg)  <math>\hat{P}\hat{T}\hat{S} = 90^\circ + \hat{S}_1</math>  <math>\hat{V}_1 = 90^\circ + \hat{S}_1</math> (ext <math>\angle \Delta</math>)  <math>\hat{V}_1 = \hat{P}\hat{T}\hat{S}</math></p> <p>OR</p> <p><math>\hat{P}_2 = 140^\circ</math> (<math>\angle</math>s on str line)  <math>\hat{W} + \hat{P}_2 = 180^\circ</math>  WVPT is cyclic quad (opp <math>\angle</math>s suppl)  <math>\hat{V}_1 = \hat{P}\hat{T}\hat{S}</math> (ext <math>\angle</math> cyclic quad)</p> <p>OR</p> <p><math>\hat{V}_1 = \hat{R}_1 + \hat{R}_2 + \hat{S}_1</math> (ext <math>\angle \Delta</math>)  <math>\hat{V}_1 = 90^\circ + \hat{S}_1</math>  <math>\hat{P}\hat{T}\hat{S} = 90^\circ + \hat{T}_2</math>  But <math>\hat{T}_2 = \hat{S}_1</math> (<math>\angle</math>s in same seg)  <math>\hat{V}_1 = \hat{P}\hat{T}\hat{S}</math></p> <p>OR</p> <p>In <math>\Delta\hat{P}\hat{T}\hat{S}</math> and <math>\Delta\hat{W}\hat{V}\hat{S}</math>  <math>\hat{P}_1 = \hat{W}</math> (<math>= 40^\circ</math>)  <math>\hat{S}_2</math> is common  <math>\hat{V}_1 = \hat{P}\hat{T}\hat{S}</math> (<math>\angle</math> sum <math>\Delta</math>)</p>	<p><math>\checkmark \hat{P}_1 = \hat{W}</math>  <math>\checkmark</math> WVPT is a cyclic quadrilateral  <math>\checkmark</math> ext <math>\angle =</math> in opp  <math>\checkmark</math> ext <math>\angle</math> cyclic quad (4)</p> <p><math>\checkmark \angle</math>s in semi circle  <math>\checkmark \hat{P}\hat{T}\hat{S} = 90^\circ + \hat{T}_2</math>  <math>\checkmark \hat{T}_2 = \hat{S}_1</math>  <math>\checkmark \angle</math>s in same seg (4)</p> <p><math>\checkmark \hat{W} + \hat{P}_2 = 180^\circ</math>  <math>\checkmark</math> WVPT is a cyclic quadrilateral  <math>\checkmark</math> opp <math>\angle</math> suppl  <math>\checkmark</math> ext <math>\angle</math> cyclic quad (4)</p> <p><math>\checkmark \hat{V}_1 = 90^\circ + \hat{S}_1</math>  <math>\checkmark \hat{P}\hat{T}\hat{S} = 90^\circ + \hat{T}_2</math>  <math>\checkmark \hat{T}_2 = \hat{S}_1</math>  <math>\checkmark \angle</math>s in same seg (4)</p> <p><math>\checkmark</math> identification of triangles  <math>\checkmark \hat{P}_1 = \hat{W}</math>  <math>\checkmark \hat{S}_2</math> is common  <math>\checkmark \angle</math> sum <math>\Delta</math> (4)</p> <p style="text-align: right;">(4) [15]</p>
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Please turn over

## QUESTION 9

9.  $\hat{C} = 90^\circ$  ( $\angle$ s in semi circle)  
 $\hat{OEA} = 90^\circ$  (corres  $\angle$ s;  $OD \parallel BC$ )  
 $AE = 8$  cm (line from circ cent  $\perp$  ch bis ch)  
 $OE = 6$  cm (Pythagoras)  
 $ED = 10 - 6$   
 $= 4$  cm



- ✓  $\hat{C} = 90^\circ$
- ✓  $\hat{OEA} = 90^\circ$
- ✓ line from circ cent  $\perp$  ch bis ch
- ✓  $OE = 6$  cm
- ✓  $ED = 4$  cm

OR

- $\hat{C} = 90^\circ$  ( $\angle$ s in semi circle)  
 $\hat{OEA} = 90^\circ$  (corres  $\angle$ s;  $OD \parallel BC$ )  
 $OE \parallel BC$  (given)  
 $OA = OB$  (radii)  
 $AE = EC = 8$  cm (midpoint theorem)  
 $OE = 6$  cm (Pythagoras)  
 $ED = 10 - 6$   
 $= 4$  cm

- ✓  $\hat{C} = 90^\circ$
- ✓  $\hat{OEA} = 90^\circ$
- ✓ midpoint theorem
- ✓  $OE = 6$  cm
- ✓  $ED = 4$  cm

OR

- $\hat{C} = 90^\circ$  ( $\angle$ s in semi circle)  
 $BC^2 = (20)^2 - (16)^2$   
 $BC^2 = 144$   
 $BC = 12$   
 $OE = \frac{1}{2} BC$  (midpoint theorem)  
 $OE = 6$  cm  
 $OD = 10$  cm  
 $ED = 10 - 6$   
 $= 4$  cm

- ✓  $\hat{C} = 90^\circ$
- ✓  $BC = 12$
- ✓ reason
- ✓  $OE = 6$  cm
- ✓  $ED = 4$  cm

[5]

OR

- $\hat{C} = 90^\circ$  ( $\angle$ s in semi circle)  
 $BC^2 = (20)^2 - (16)^2$   
 $BC^2 = 144$   
 $BC = 12$   
 $OE = \frac{1}{2} BC$  (midpoint theorem)  
 $OE = 6$  cm  
 $ED = 4$  cm

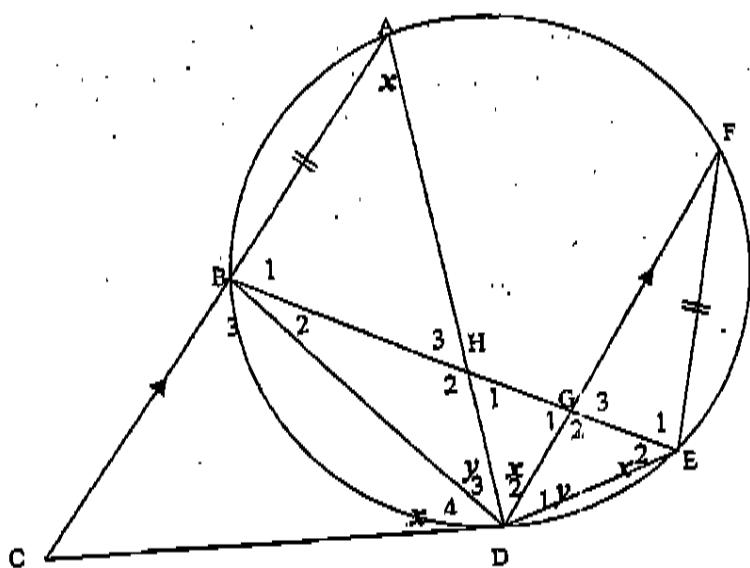
- ✓  $\hat{C} = 90^\circ$
- ✓  $BC = 12$
- ✓ reason

- ✓  $OE = 6$  cm
- ✓  $ED = 4$  cm

[5]

MS

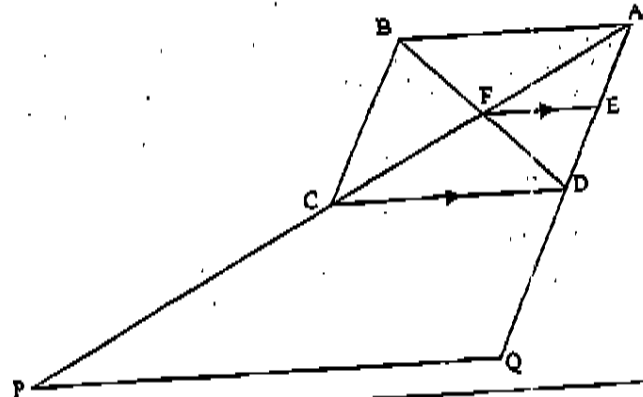
QUESTION 10



<p>10.1</p>	<p><math>\hat{A} = \hat{D}_1 = x</math> (tan ch th)  <math>\hat{E}_2 = x</math> (tan ch th). OR (<math>\angle</math>s in same seg)  <math>\hat{D}_2 = \hat{A} = x</math> (alt <math>\angle</math>s; CA <math>\parallel</math> DF)</p>	<p>✓ <math>\hat{A} = x</math>                  ✓ tan ch th                  ✓ <math>\hat{E}_2 = x</math>                  ✓ reason                  ✓ <math>\hat{D}_2 = x</math>                  ✓ alt <math>\angle</math>s; CA <math>\parallel</math> DF                  (6)</p>
<p>10.2</p>	<p>In <math>\triangle BHD</math> and <math>\triangle FED</math>                  1. <math>\hat{B}_2 = \hat{F}</math> (<math>\angle</math>s in same seg)                  2. <math>\hat{D}_3 = \hat{D}_1</math> (= chs subt = <math>\angle</math>s)   <math>\triangle BHD \parallel \triangle FED</math> (<math>\angle\angle\angle</math>)</p>	<p>✓ <math>\hat{B}_2 = \hat{F}</math>                  ✓ <math>\angle</math>s in same seg                  ✓ <math>\hat{D}_3 = \hat{D}_1</math>                  ✓ = chs subt = <math>\angle</math>s                  ✓ <math>\angle\angle\angle</math>                  (5)</p>
<p>10.3</p>	<p><math>\frac{FE}{BH} = \frac{FD}{BD}</math> (<math>\parallel \Delta</math>s)                  But FE = AB (given)  <math>\frac{AB}{BH} = \frac{FD}{BD}</math>                  AB.BD = FD.BH</p>	<p>✓ <math>\frac{FE}{BH} = \frac{FD}{BD}</math>                  ✓ FE = AB                  (2)                   [13]</p>

*MS*

QUESTION 11



11.1	$AF = FC$ $FE \parallel CD$ $AE = ED$ (diags of parallelogram bisect) (Prop Th; $FE \parallel CD$ ) OR (Midpoint Theorem)	$\checkmark AF = FC$ $\checkmark$ reason (2)
11.2	$\frac{AC}{CP} = \frac{1}{2}$ (given) $\frac{AD}{DQ} = \frac{1}{2}$ (given) $\frac{AC}{CP} = \frac{AD}{DQ}$ $CD \parallel PQ$ (converse proportionality theorem) $CD \parallel FE$ (given) $\therefore PQ \parallel FE$ OR $\frac{AC}{AP} = \frac{1}{3}$ $\frac{AD}{AQ} = \frac{1}{3}$ $\frac{AC}{AP} = \frac{AD}{AQ}$ $CD \parallel PQ$ (converse proportionality theorem) $CD \parallel FE$ (given) $\therefore PQ \parallel FE$ OR $\frac{AF}{AP} = \frac{1}{6}$ $\frac{AE}{AQ} = \frac{1}{6}$ $\frac{AF}{AP} = \frac{AE}{AQ}$ $\therefore PQ \parallel FE$ (converse proportionality theorem)	$\checkmark$ ratios equal $\checkmark CD \parallel PQ$ $\checkmark$ reason: converse prop th and conclusion (3)  $\checkmark$ ratios equal $\checkmark CD \parallel PQ$ $\checkmark$ reason: converse prop th and conclusion (3)  $\checkmark \frac{AF}{AP} = \frac{1}{6}$  $\checkmark \frac{AF}{AP} = \frac{AE}{AQ}$ $\checkmark$ conv prop theorem

*Handwritten signatures and marks.*

<p>11.3</p> <p>In <math>\triangle AEF</math> and <math>\triangle APQ</math></p> <ol style="list-style-type: none"> <li><math>\hat{A}</math> is common</li> <li><math>\hat{A}EF = \hat{A}QP</math> (corres <math>\angle</math>s; <math>FE \parallel PQ</math>)</li> <li><math>\hat{A}FE = \hat{A}PQ</math> (corres <math>\angle</math>s; <math>FE \parallel PQ</math>)</li> </ol> <p><math>\therefore \triangle AEF \parallel \triangle APQ</math> (<math>\angle\angle\angle</math>)</p> $\frac{FE}{PQ} = \frac{AF}{AP} \quad (\parallel \Delta\text{s})$ $\frac{FE}{60} = \frac{1}{6}$ <p><math>FE = 10 \text{ cm}</math></p> <p><b>OR</b></p> <p>In <math>\triangle ADC</math> and <math>\triangle APQ</math></p> <ol style="list-style-type: none"> <li><math>\hat{A}</math> is common</li> <li><math>\hat{A}DC = \hat{A}QP</math> (corres <math>\angle</math>s; <math>CD \parallel PQ</math>)</li> <li><math>\hat{A}CD = \hat{A}PQ</math> (corres <math>\angle</math>s; <math>CD \parallel PQ</math>)</li> </ol> <p><math>\therefore \triangle ADC \parallel \triangle APQ</math> (<math>\angle\angle\angle</math>)</p> $\frac{AC}{AP} = \frac{AD}{AQ} = \frac{1}{3} \quad (\parallel \Delta\text{s})$ $CD = \frac{1}{3} PQ$ <p><math>CD = 20 \text{ cm}</math></p> <p>But <math>AF = FC</math> <math>AE = ED</math> (Midpoint Theorem)</p> $FE = \frac{1}{2} CD$ <p><math>FE = 10 \text{ cm}</math></p>	<p>✓ first pair of angles equal with reason ✓ second pair of angles equal with reason</p> <p>✓ <math>\frac{AF}{AP} = \frac{1}{6}</math> ✓ <math>\frac{FE}{PQ} = \frac{AF}{AP}</math> ✓ answer (5)</p> <p>✓ first pair of angles equal with reason ✓ second pair of angles equal with reason</p> <p>✓ <math>CD = \frac{1}{3} PQ</math></p> <p>✓ <math>FE = \frac{1}{2} CD</math> ✓ answer (5)</p> <p><b>[10]</b></p>
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TOTAL: 100